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AXIONS & NON-LINEARITIES

WITH P. SOLER & F. CEFALA – TO APPEAR

Warsaw, String Pheno 2018

STANDARD ALP MODELS - MISALIGNMENT

Abbott, Sikivie;
Preskill, Wise, Wilczek;
Dine, Fischler

Random field value [after inflation], ϕ_i

$$\text{E.o.M: } \ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

3 phases:

$$t \ll t_1$$

$$3H \gg m$$

field becomes overdamped,
gets frozen

$$t \simeq t_1$$

$$3H \simeq m$$

damping undercritical,
oscillations begin

$$t \gg t_1$$

$$3H \ll m$$

indistinguishable from
pressureless gas

STANDARD ALP MODELS

Abbott, Sikivie;
Preskill, Wise, Wilczek;
Dine, Fischler

$$V(\phi) = \Lambda^4 \left[1 - \cos\left(\frac{\phi}{f}\right) \right]$$

$$m^2 = \frac{\Lambda^4}{f^2}$$

$$|\phi| \lesssim \pi f$$

$$\mathcal{L} \supset \frac{\phi}{f} F \tilde{F}, \frac{\partial_\mu \phi}{f} \bar{\psi} \gamma^\mu \gamma^5 \psi$$

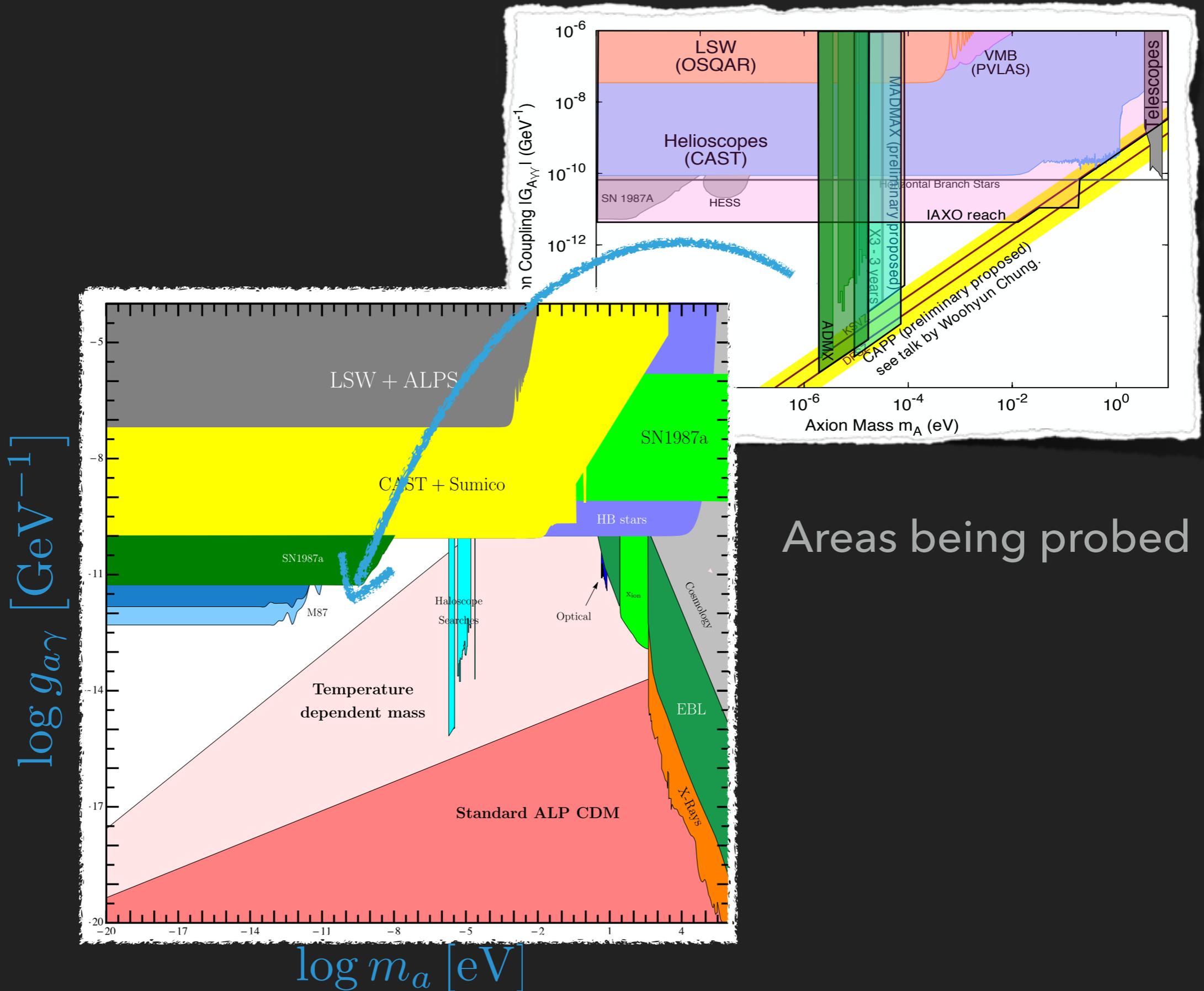
$$g \equiv \frac{\alpha}{2\pi} \frac{1}{f} \mathcal{N}$$

CURRENT LIMITS

ALPS

RUNNING EXPERIMENTS:

- IAXO
- MADMAX
- ADMX
- ETC...



Areas being probed

CURRENT LIMITS

ALPS

RUNNING

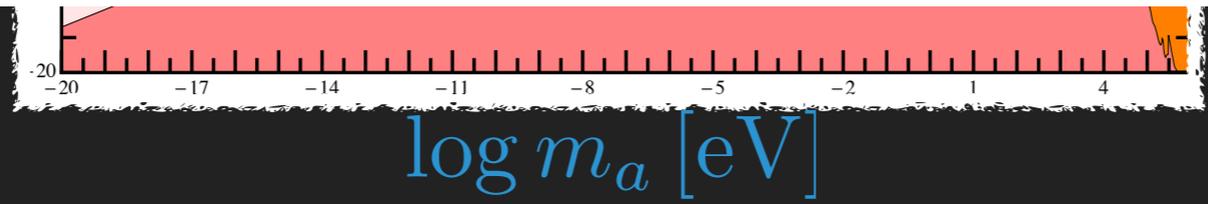
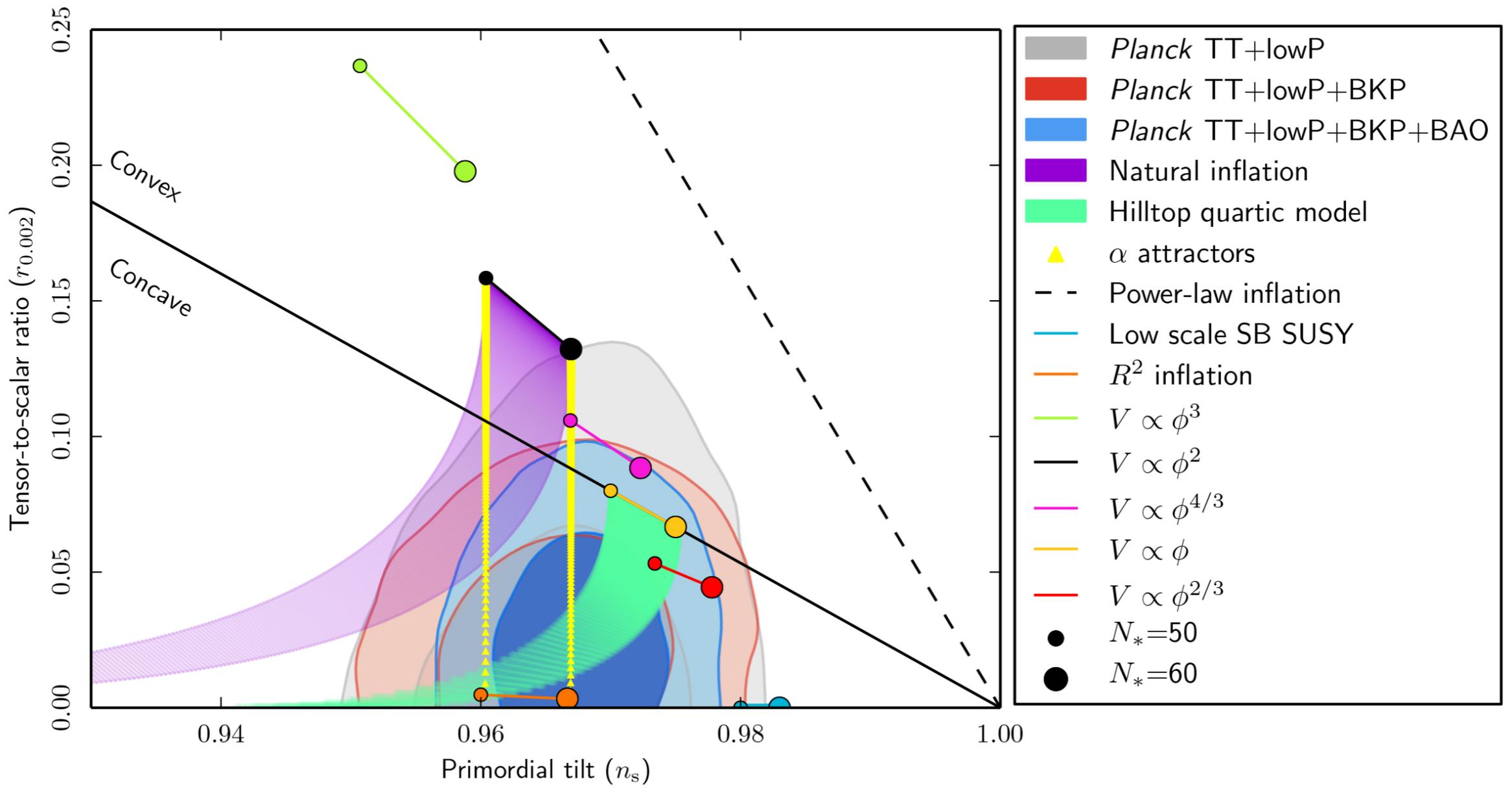
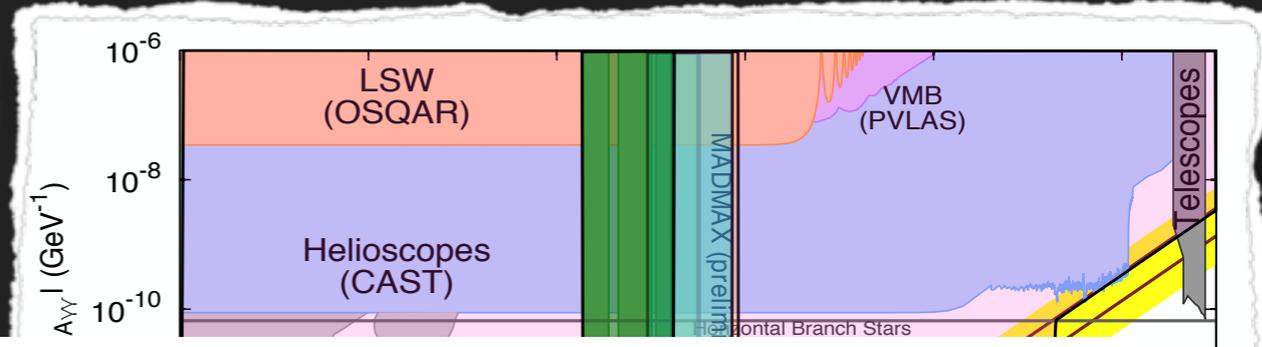
EXP

-IA

-M

-AL

-ET



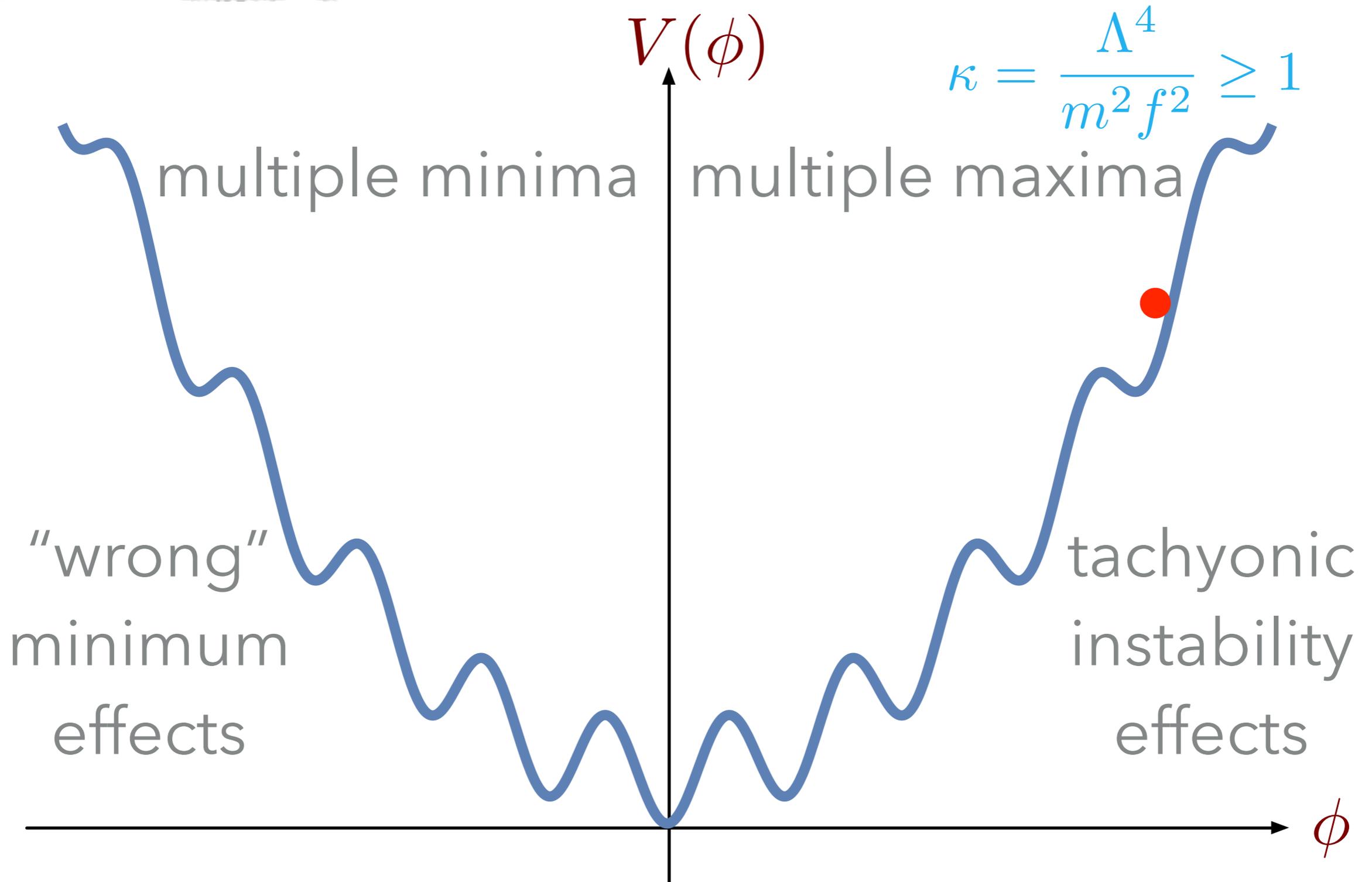
bed

AXION MONODROMY

POTENTIAL

Silverstein, Westphal,
McAllister;
Kim, Nilles, Peloso

$$V(\phi) = \frac{1}{2}m^2\phi^2 + \Lambda^4 \left(1 - \cos \left(\frac{\phi}{f} \right) \right)$$



LINEAR REGIME

- ▶ Monodromy Dark Matter
 - ▶ Tachyonic instabilities
 - ▶ Parametric resonance
 - ▶ Saturation of DM abundance
- ▶ Dynamical Phase Decomposition
 - ▶ "wrong minimum" effects
 - ▶ Gravitational waves

Jaeckel, VMM,
Witkowski

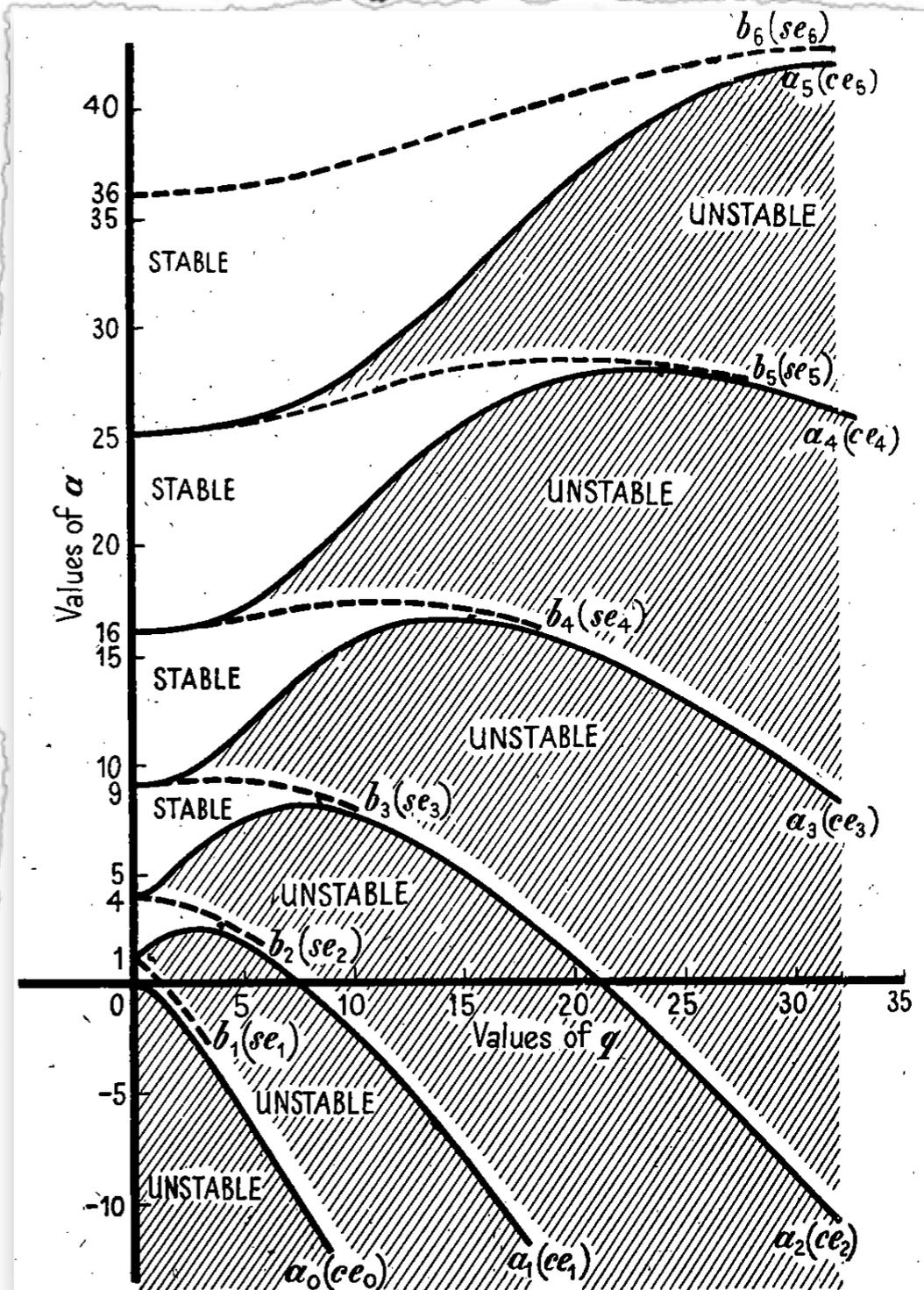
Hebecker, et al.

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stability/instability bands

LINEAR REGIME

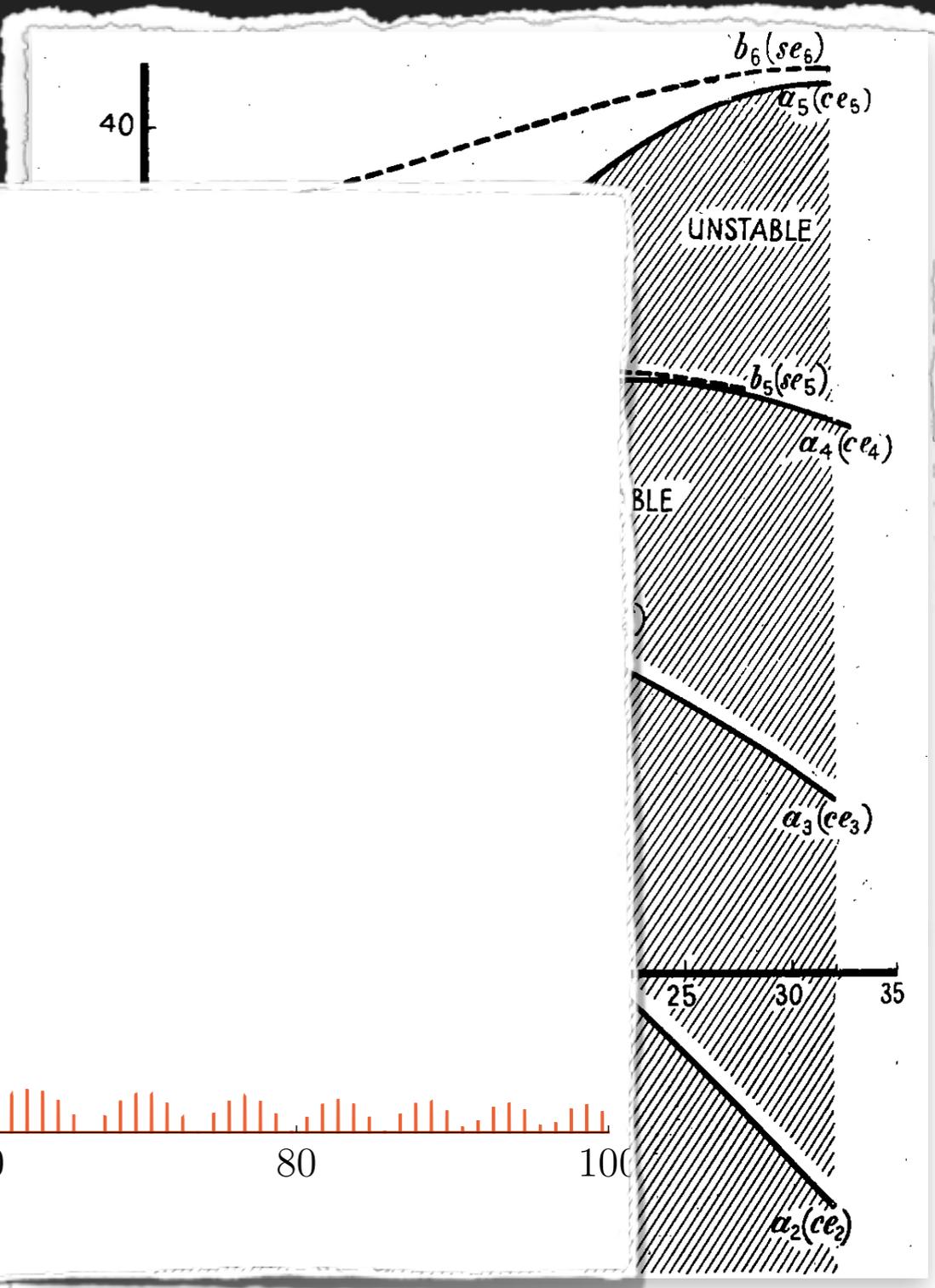
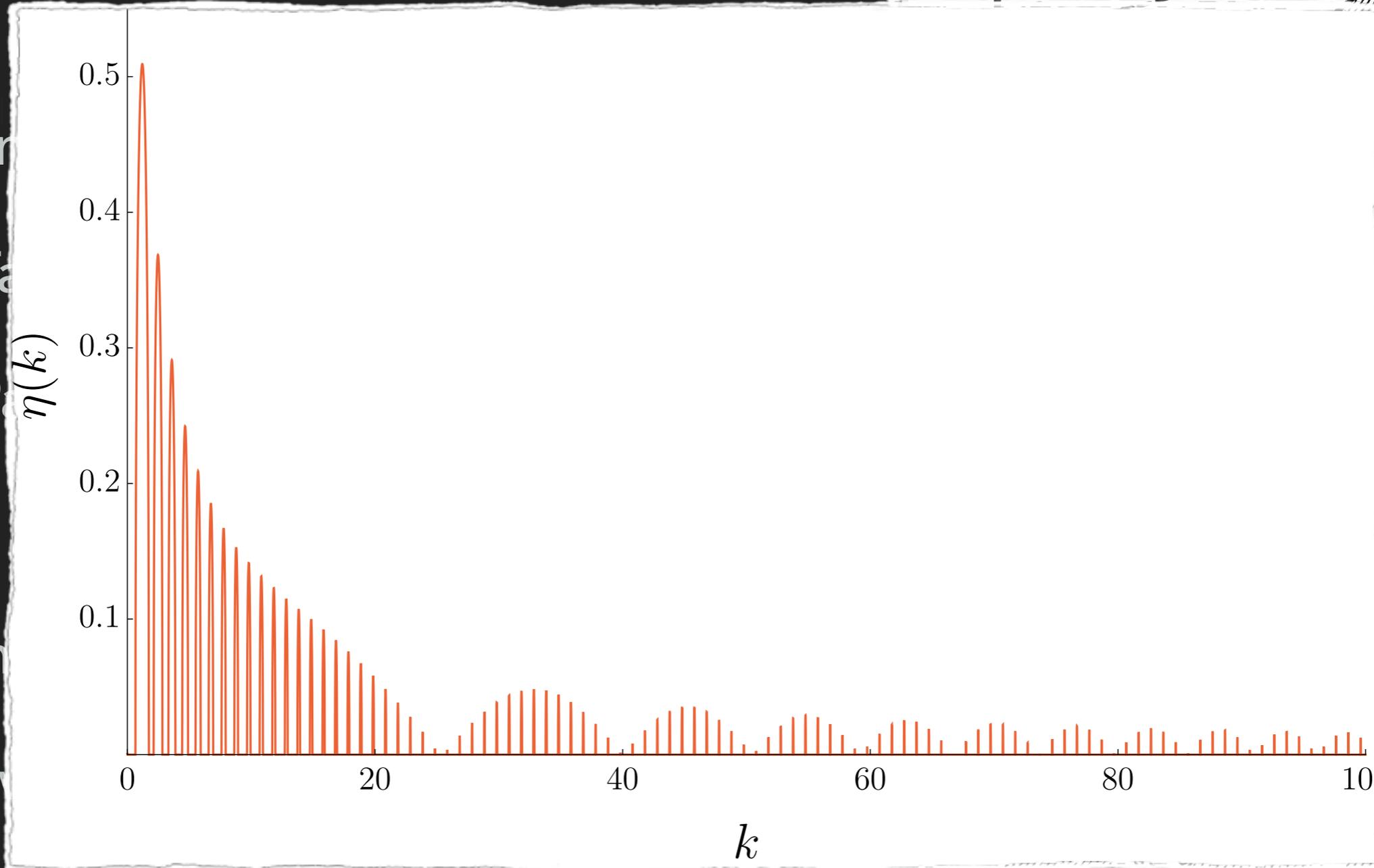
▶ Monodromy

▶ Tachyons

▶ Poles

▶ Dynamics

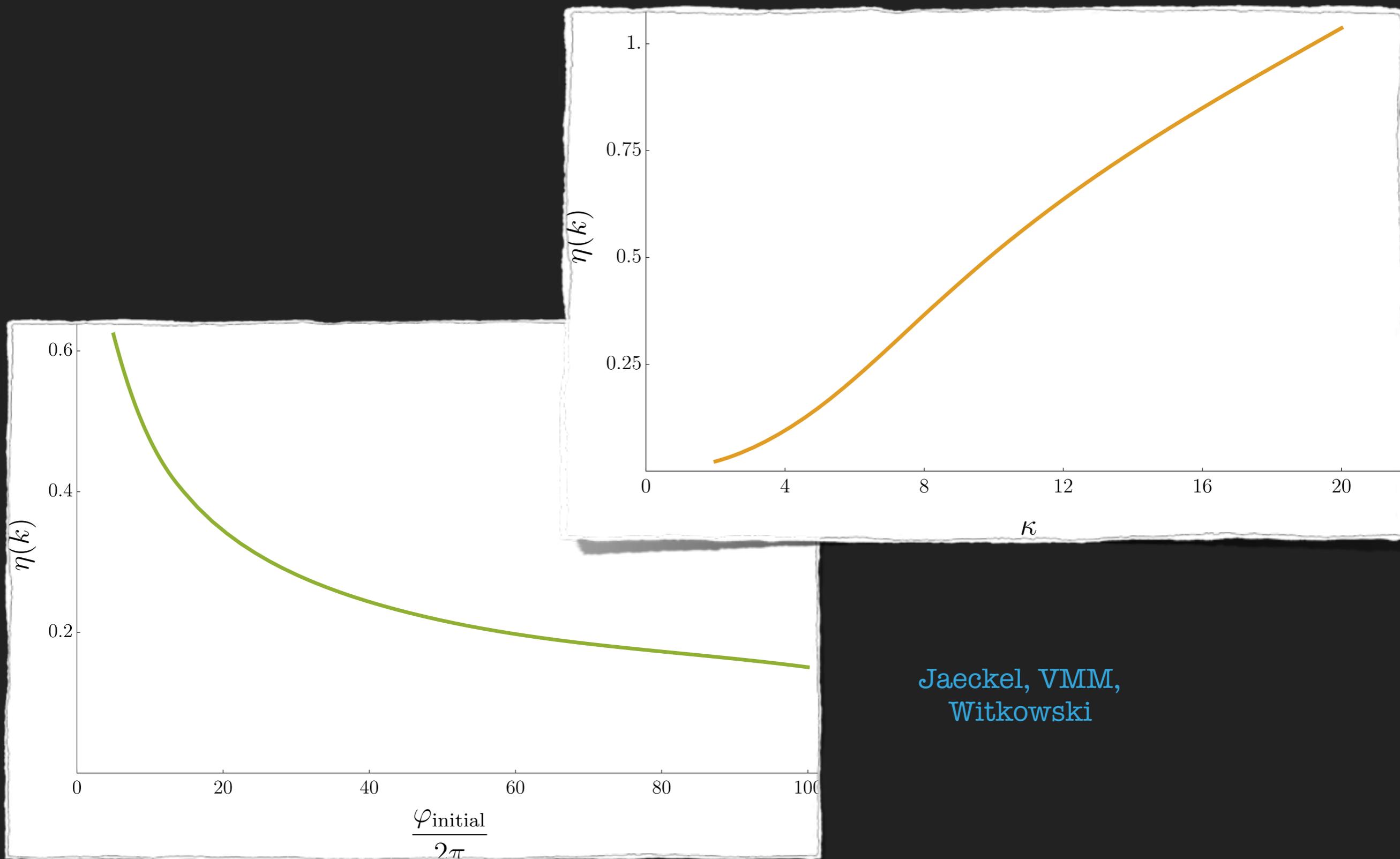
▶ “



▶ Gravitational waves

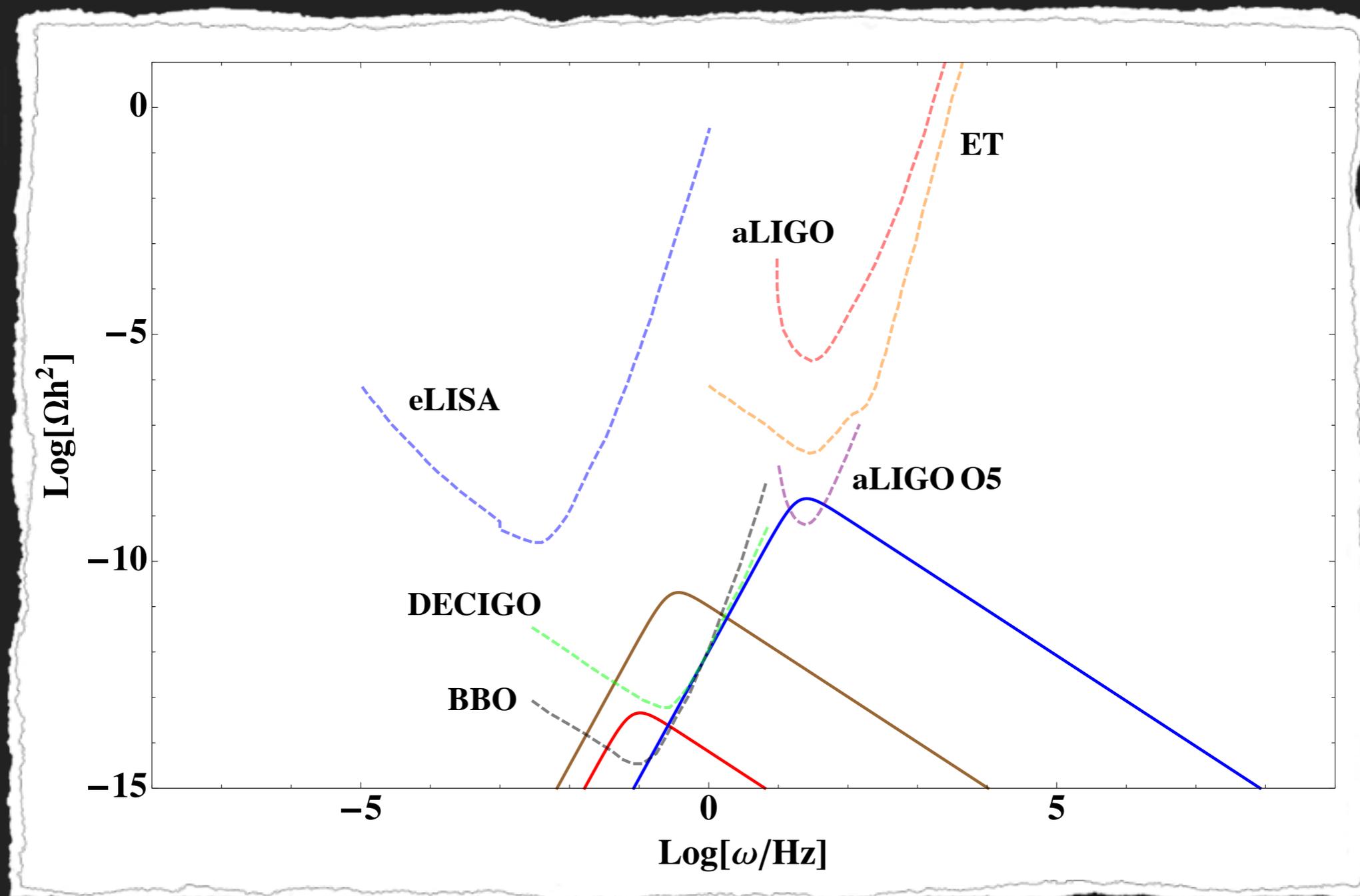
stability/instability bands

LINEAR REGIME - GROWTH OF FLUCTUATIONS

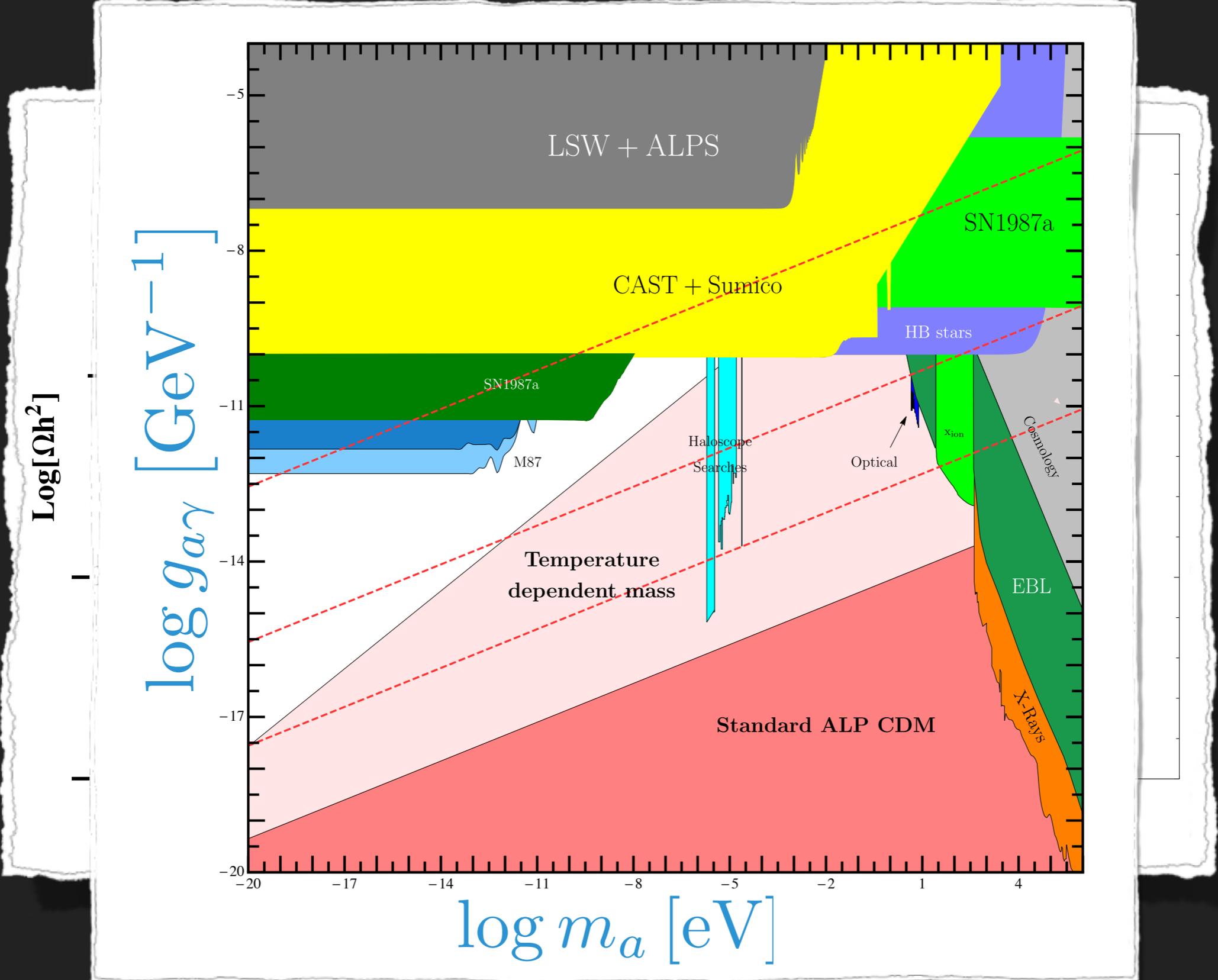


Jaeckel, VMM,
Witkowski

EXPERIMENTAL ACCESSIBILITY



EXPERIMENTAL ACCESSIBILITY



SETUP

Lattice simulations using modified **LATTICEEASY** code in 2+1d with 512^2 lattice points

$$\ddot{\phi} + 3H\dot{\phi} - \frac{\nabla^2}{a^2}\phi + \frac{\partial V}{\partial\phi} = 0$$

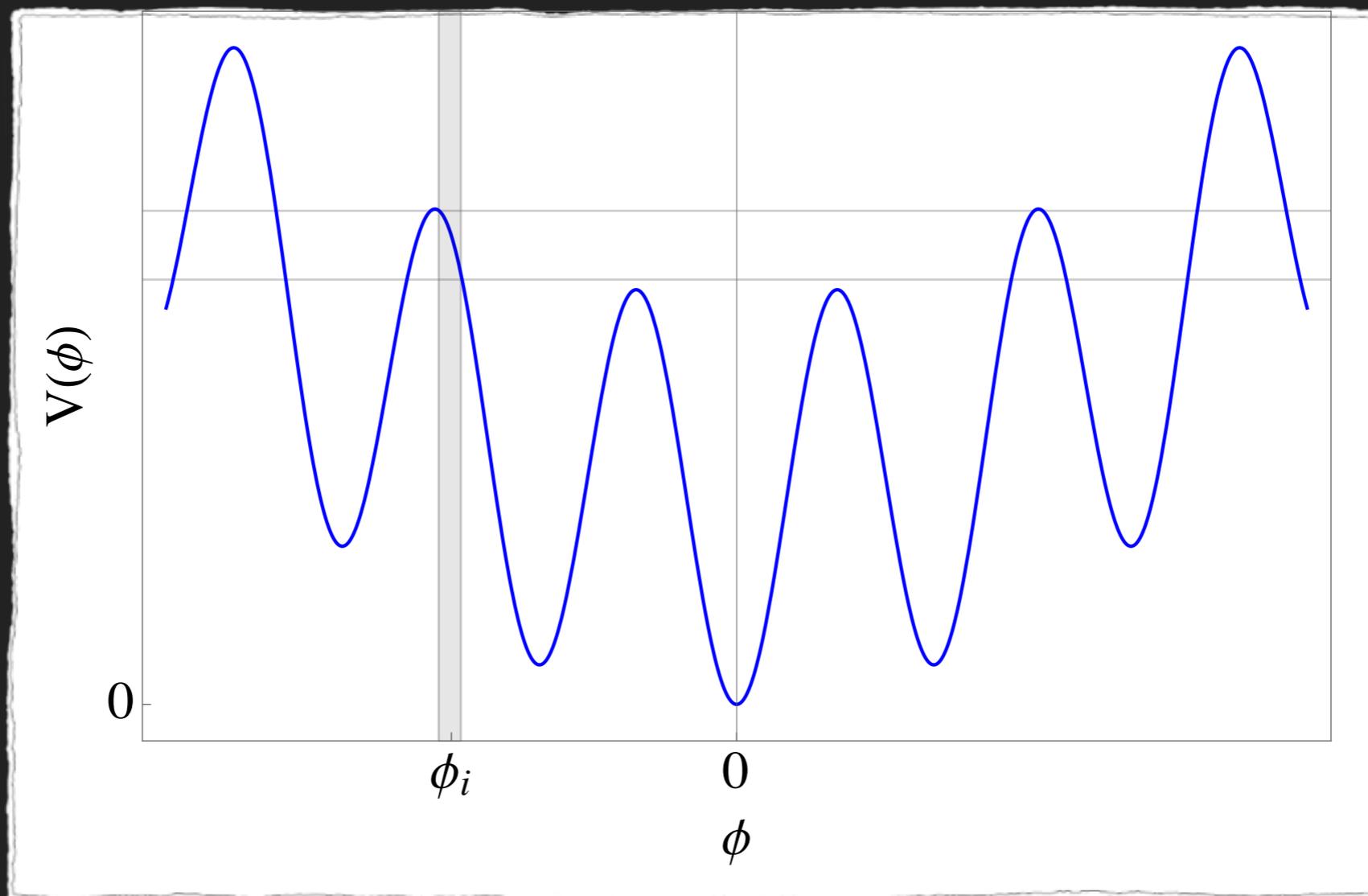
$$H^2 = \frac{1}{3M_{\text{P}}^2} \left(V + \frac{1}{2}\dot{\phi}^2 + \frac{1}{2a^2}|\nabla\phi|^2 \right)$$

Comoving volume:

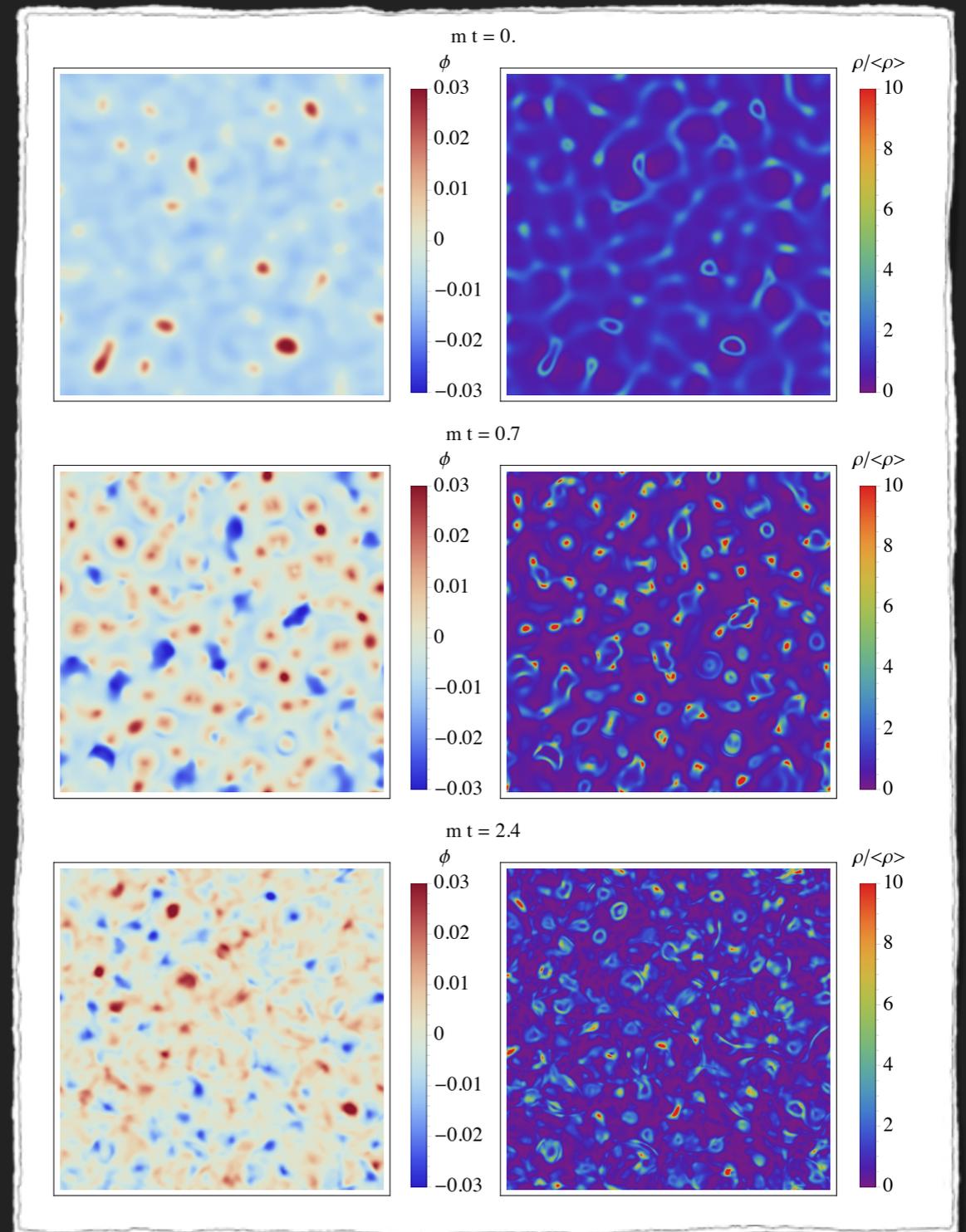
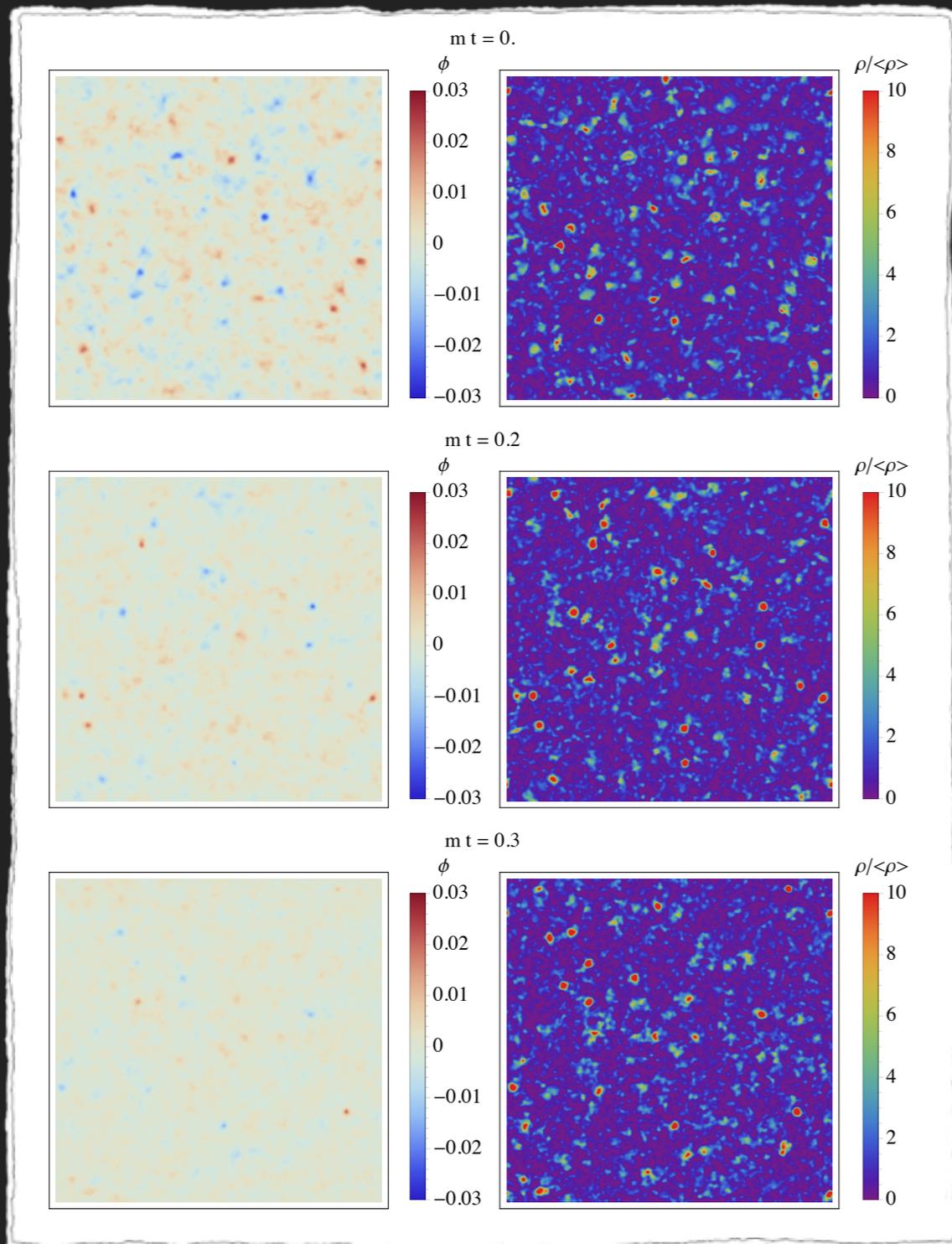
$$\mathcal{V} = L^2 = \left(\frac{H_i^{-1}}{5} \right)^2$$

$$H_i = \sqrt{V(\phi_i)/3}$$

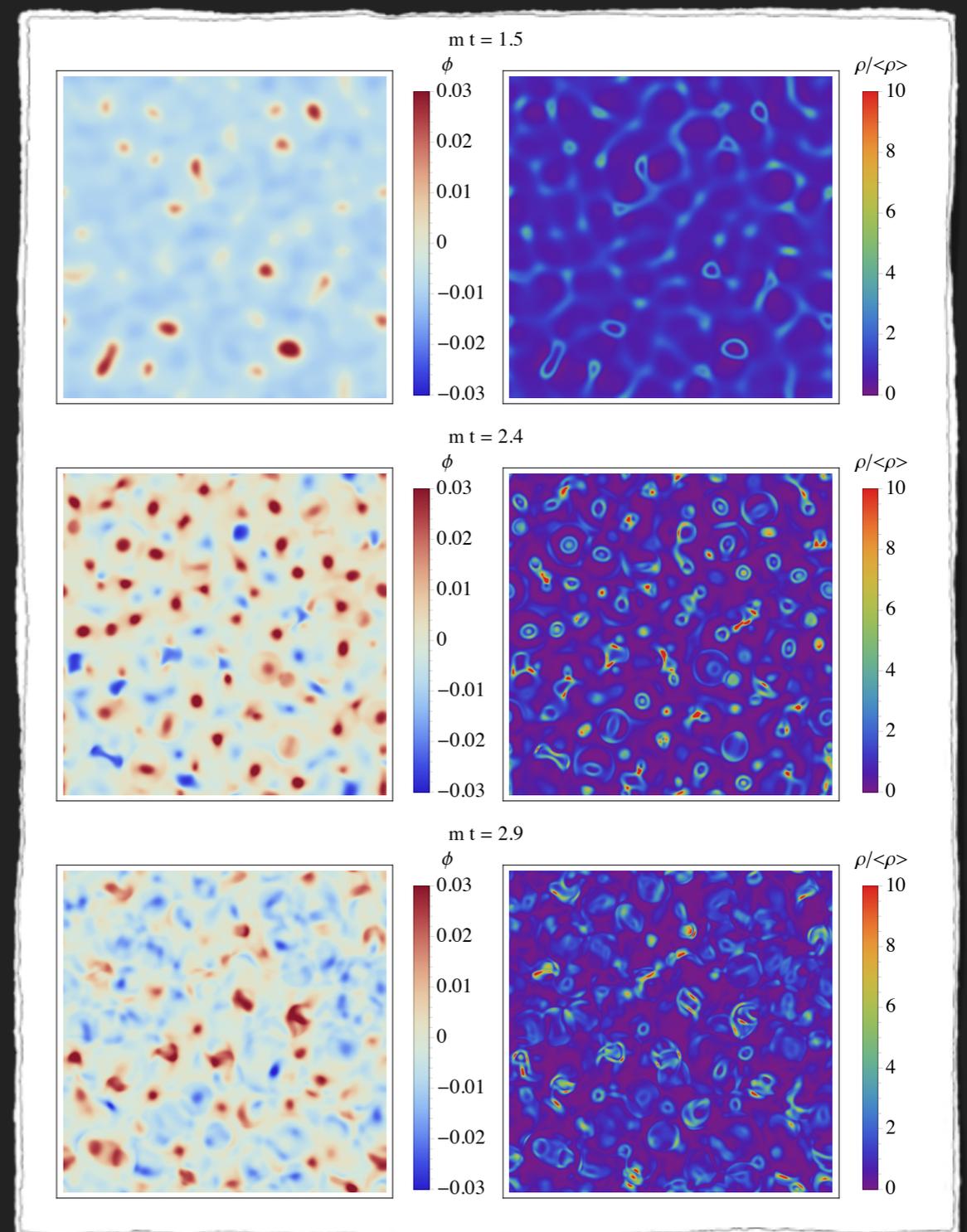
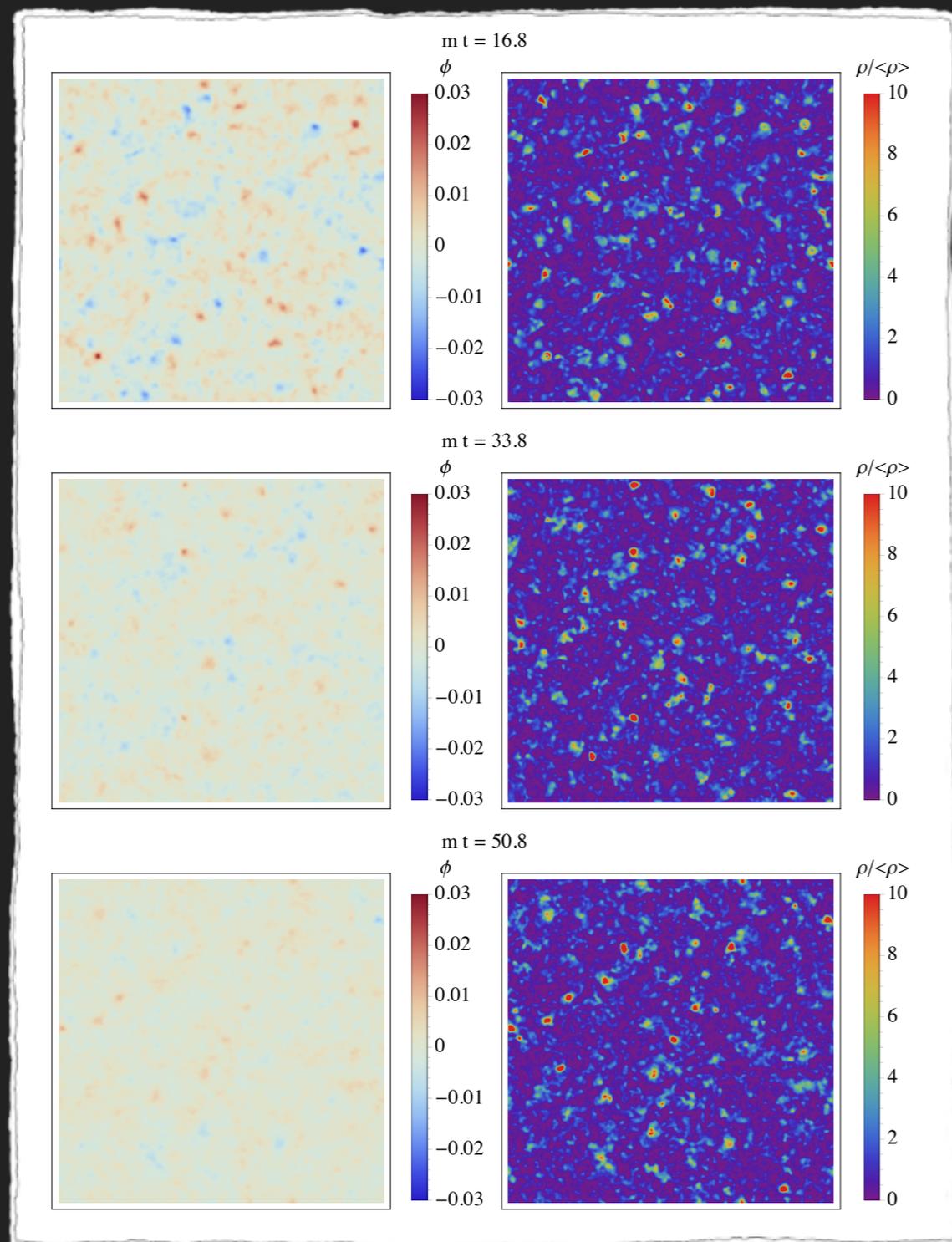
MONODROMY



MONODROMY

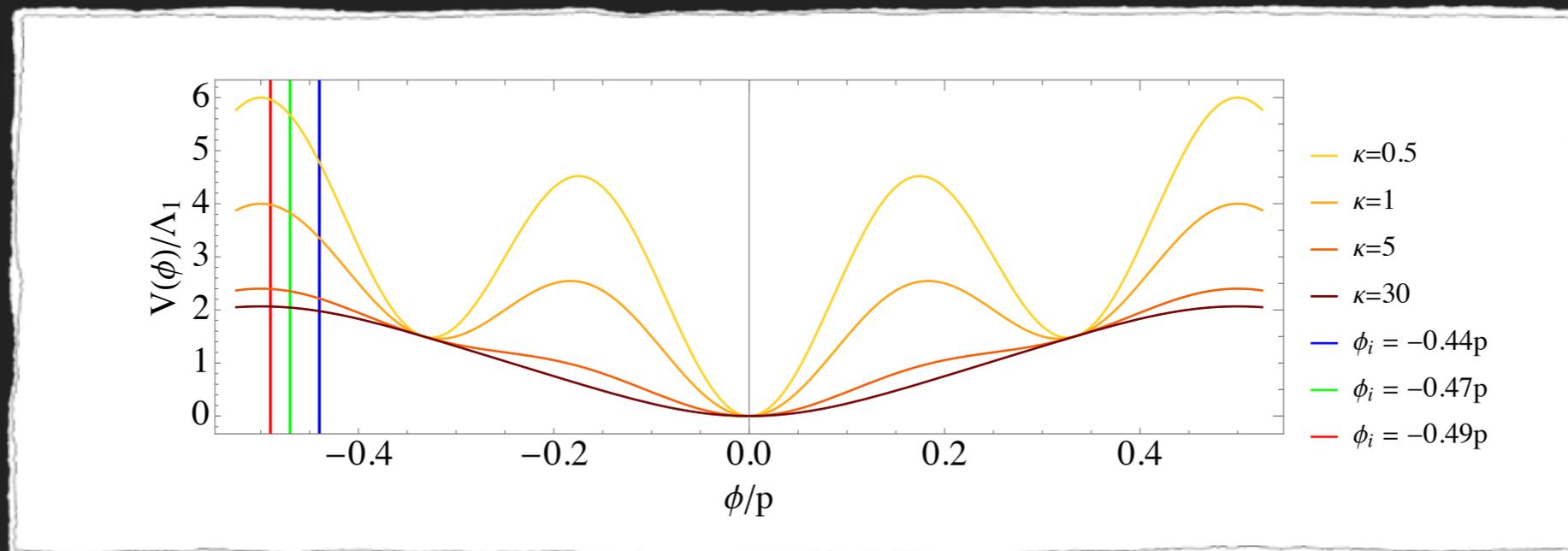


MONODROMY



INSTANTON CORRECTIONS

$$\sum_{i=1}^n \Lambda_n^4 \left[1 - \cos \left(\frac{n\phi}{f} \right) \right]$$

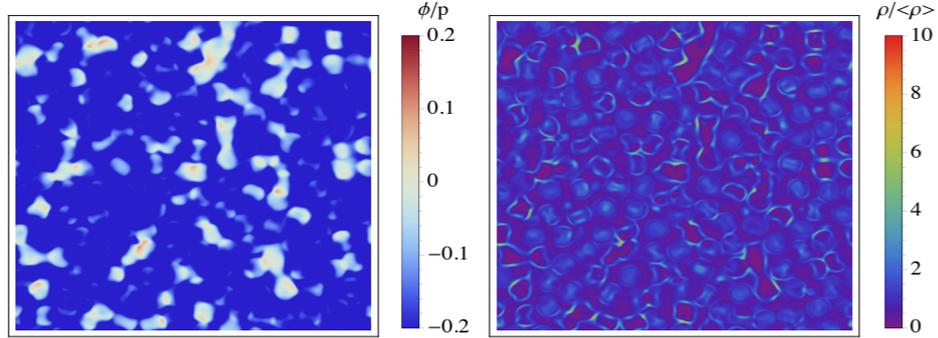


$$\kappa \equiv \frac{\Lambda_1^4}{\Lambda_n^4}$$

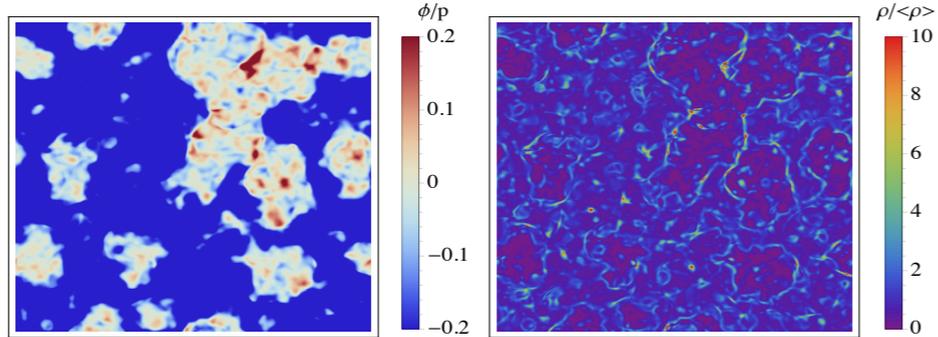
INSTANTON CORRECTIONS

$$\phi_i = -0.49p, \Lambda_1 = 0.5 \Lambda_2$$

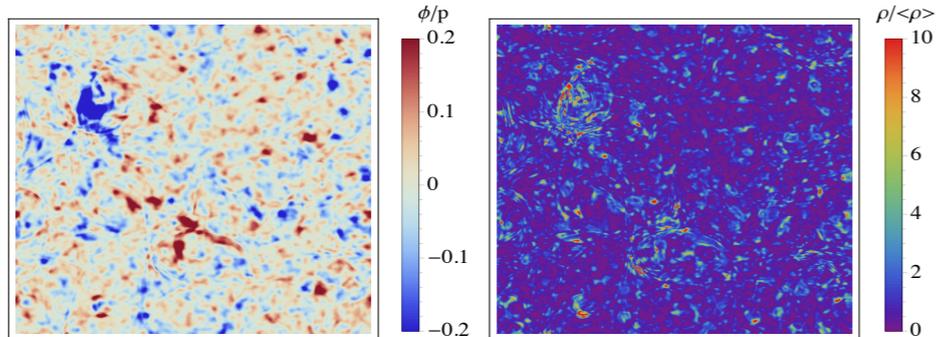
m t = 36.6



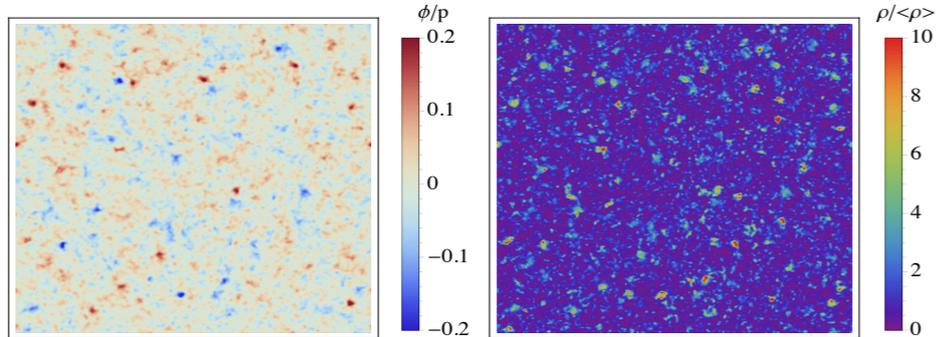
m t = 49.7



m t = 102.

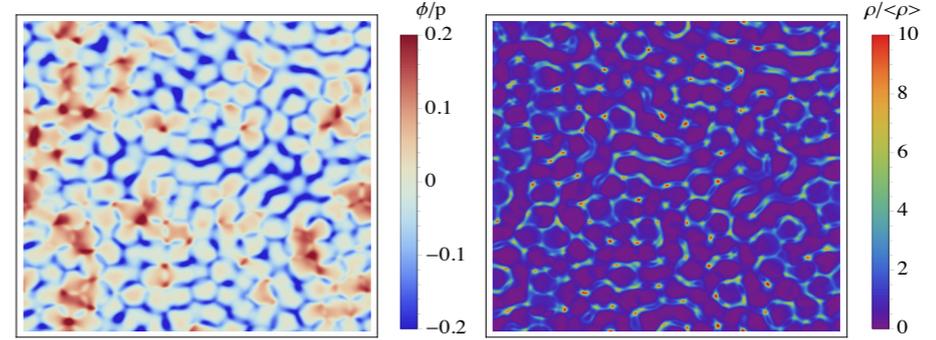


m t = 435.8

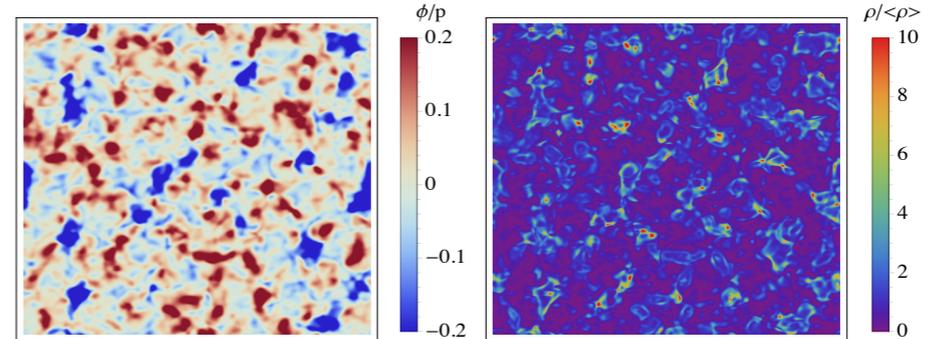


$$\phi_i = -0.49p, \Lambda_1 = 1 \Lambda_2$$

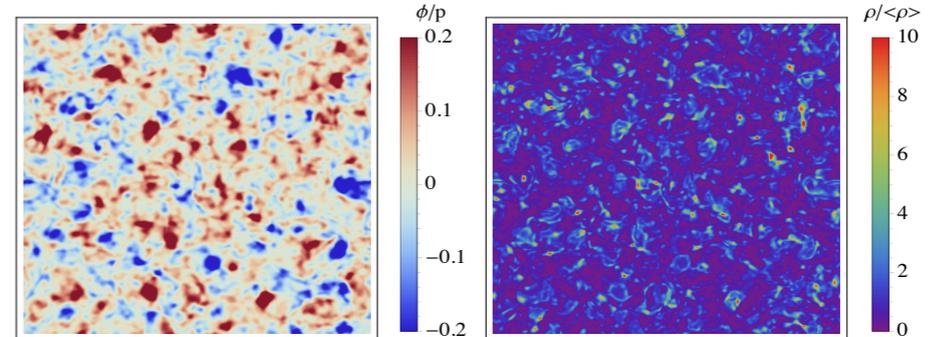
m t = 44.6



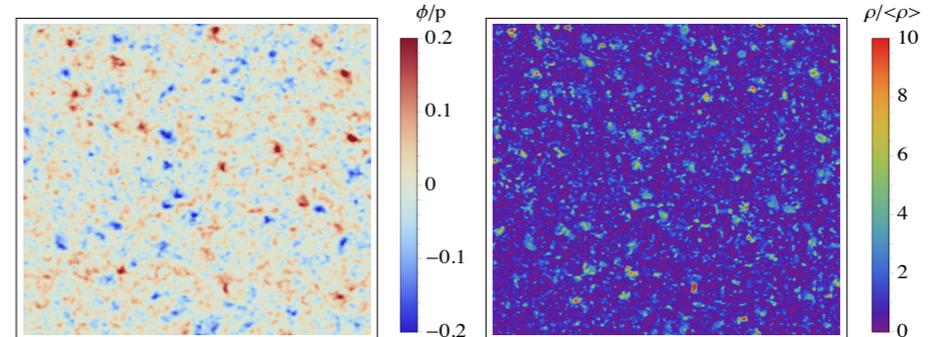
m t = 53.9



m t = 72.4



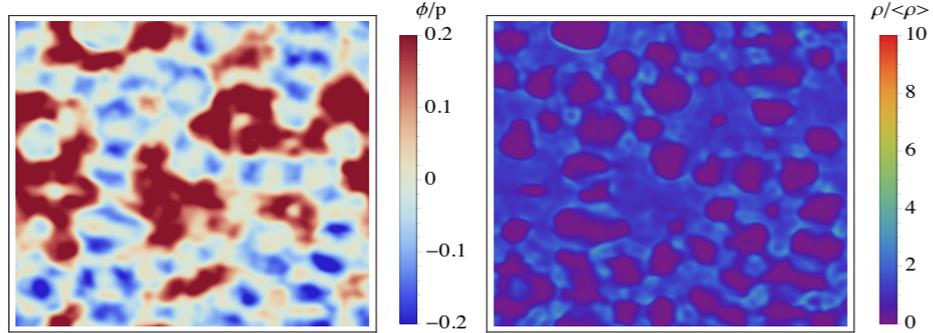
m t = 316.2



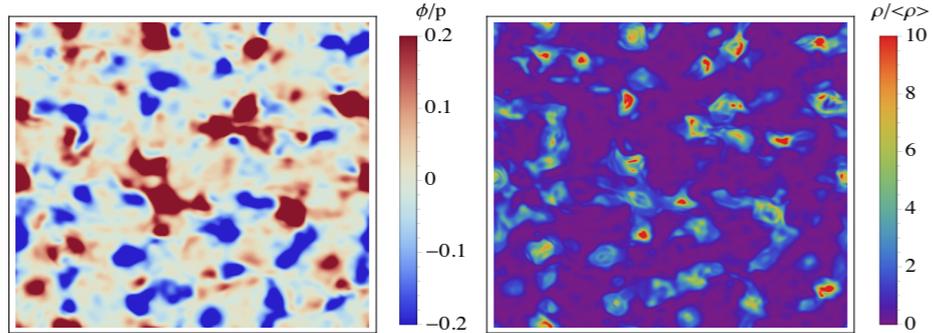
INSTANTON CORRECTIONS

$$\phi_i = -0.49\rho, \Lambda_1 = 5 \Lambda_2$$

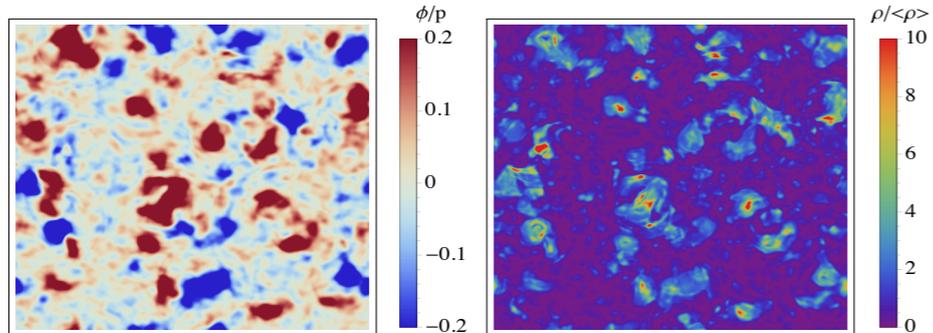
m t = 141.6



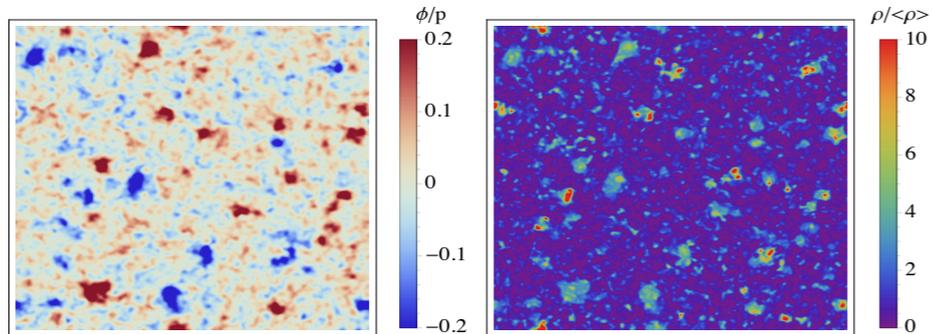
m t = 155.9



m t = 187.5

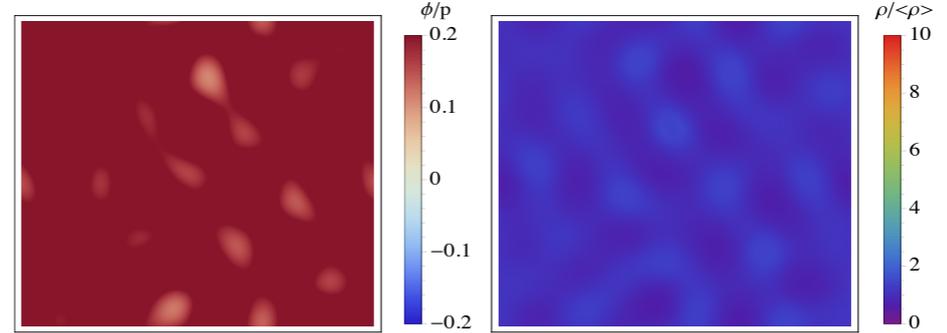


m t = 334.7

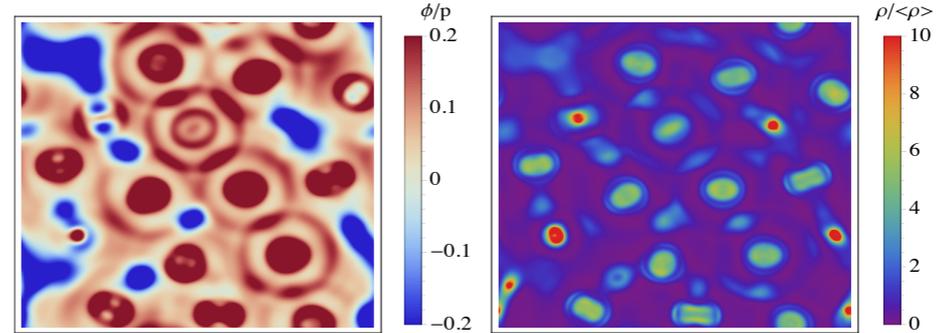


$$\phi_i = -0.47\rho, \Lambda_1 = 30 \Lambda_2$$

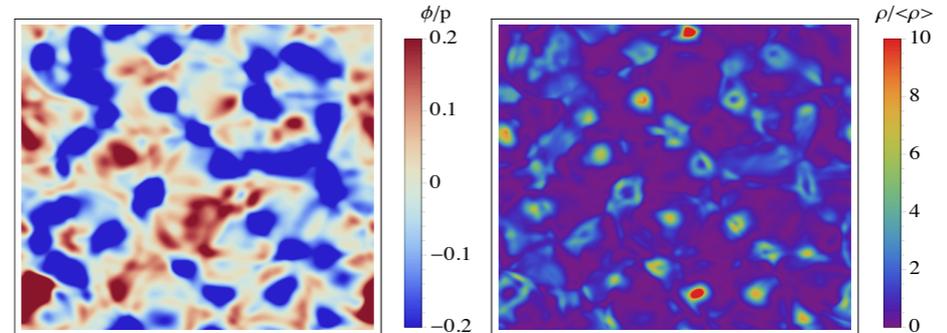
m t = 41.2



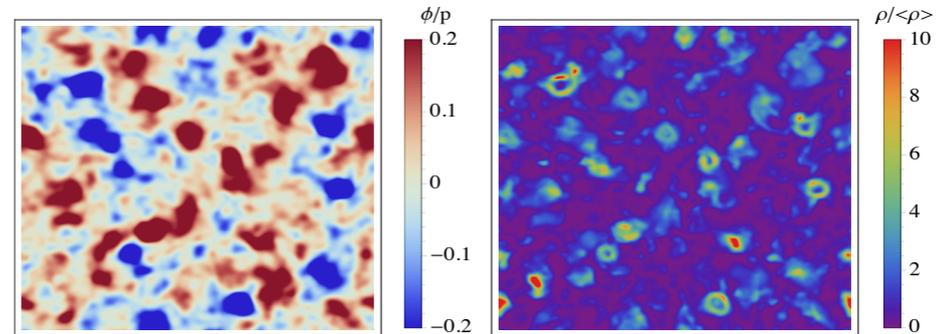
m t = 55.2



m t = 69.3



m t = 114.



AXIONS & NON-LINEAR EFFECTS

- ▶ 2+1 lattice simulations show appearance of oscillons
 - ▶ oscillons are long-lived stable objects [Amin; Muia, et al.](#)
- ▶ 3+1 lattice simulations confirm appearance
- ▶ Oscillons generic for $\kappa > 1$ monodromy potentials
- ▶ Also seemingly generic for corrected potential
- ▶ Post-reheating, accessible effects washed out

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Thanks!